

Sample Exam 1 - Systems of Equations

You will have 30 minutes to complete the exam. You may use a calculator, but you must show all steps done to get full credit for completing the problem. This means that if you use your calculator for anything other than arithmetic, you must indicate on your test paper what you did on the calculator.

1. Consider a degree 4 polynomial  $p(x) = p_0 + p_1x + p_2x^2 + p_3x^3 + p_4x^4$  which passes through the points  $(-2,-1)$ ,  $(-1,-8)$ ,  $(0,0)$ ,  $(1,4)$ , and  $(2,0)$ . Write, but **do not solve**, a system of linear equations, in standard form, that can be solved to find the coefficients of  $p(x)$ .
2. Solve the system of equations below. Make sure at each step you indicate what you are doing.

$$2x + 2y + 4z = 10$$

$$2x - y + z = 1$$

$$-3x + y + 3z = -6$$

3. (TRUE or FALSE) Consider the following statement and decide if it is true or false. If it is true, provide reasoning. If it is false, provide a counterexample.

“If the reduced row-echelon form of the **coefficient matrix** has a pivot in every column, then the system has a unique solution.”

4. How many solutions does the following system of equations have? Be sure to back up your answer with an explanation.

$$2x + 12y - 6z = 6$$

$$y - 5z = -7$$

$$-3x - 22y + 29z = -15$$